



COURSE SYLLABUS

Course: Probability and Statistics
Number: Math 315
Credit-Hours: 3 credits [semester credit hours]

Course Description: Emphasizes probability, probability density functions, distributions, statistical inferences and estimation, correlation, and regression.

Prerequisites: Successful completion (C- or higher) of MATH 214 (Calculus II) or equivalent.

Course Workload: 3 semester credit hours • 3 student work hours per credit hour • 14 week Carnegie semester = 126 hours student course workload average

Examination Requirements: Proctored written final examination must be passed at 60% or higher to earn passing grade in course. "B" and "A" grade paths have additional examinations. See <http://www.distancecalculus.com/grades/> for more information.

Course Professor: Robert R. Curtis, Ph.D. <robert@distancecalculus.com>

University Information: Roger Williams University, University College, 1 Empire Plaza, Providence, RI, USA 02903. Accredited by New England Commission of Higher Education (NECHE). See <https://www.rwu.edu/academics/accreditations> for more information.

E-Textbook: "Probability, Statistics & LiveMath" by Davis/Porta/Uhl et al
Mathematics Software: LiveMath™ Computer Algebra & Graphing System
and/or Mathematica™ Computer Algebra & Graphing System

Detailed Syllabus

1. Getting Started
 - 1.1. Email and Chat
 - 1.2. Learning About the Course
 - 1.3. Required Hardware
 - 1.4. Software Fundamentals

2. Simulations
 - 2.1. Uniform Distributions
 - 2.2. Monte Carlo Methods
 - 2.3. Random Walks
 - 2.4. Shooting craps; Iterated Fractals.

3. Data Analysis
 - 3.1. Frequency
 - 3.2. Expected Value
 - 3.3. Cumulative Distributions
 - 3.4. Variance
 - 3.5. Histograms
 - 3.6. Related formulas for Expected Values and Variance

4. Probabilities
 - 4.1. Calculating Probability
 - 4.2. Union and Intersection and Probability
 - 4.3. Conditional Probability Formula
 - 4.4. Independence
 - 4.5. Indicator functions

5. More Data Analysis
 - 5.1. Markov's Inequality
 - 5.2. Chebyshev's Theorem
 - 5.3. Laws of Large Numbers
 - 5.4. One-Sided Chebyshev Theorem

6. Normal and Exponential Distributions
 - 6.1. Approximately Normally Distributed Sets
 - 6.2. Normal Distribution
 - 6.3. Approximately Exponentially Distributed Sets
 - 6.4. Exponential Distribution
 - 6.5. Memoryless Property of Exponential Distributions

7. Random Variables

- 7.1. "Random Variables"
- 7.2. Discrete Random Variables
- 7.3. Continuous Random Variables
- 7.4. Probability Density Functions
- 7.5. Cumulative Distribution Functions
- 7.6. Expected Values and Variance
- 7.7. Markov, Chebyshev, and Law of Large Numbers Revisited
- 7.8. Mean, Median, and Mode

8. Joint Distributions

- 8.1. Joint Probability Calculations
- 8.2. Discrete & Continuous
- 8.3. Expected Values, Covariance, and Correlation.
- 8.4. Conditional Probability Calculations
- 8.5. Conditional Expectations
- 8.6. The Law of Total Probability

9. Central Limit Theorem

- 9.1. Generating Functions for Discrete Random Variables
- 9.2. Generating Functions for Continuous Random Variables
- 9.3. Generating Functions and Independence
- 9.4. Central Limit Theorem
- 9.5. Fourier Transforms
- 9.6. Chi-squared and Gamma random variables

Additional Optional Modules:

10. Counting

- 10.1. Binomial and Poisson counting
- 10.2. Binomial and Poisson Distributions

11. Statistics

- 11.1. Sampling
- 11.2. Confidence Intervals
- 11.3. Hypothesis testing